

FX Single Pin Barrier Option Product Specification

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Chapter 1

FX Single Pin Barrier Option

1.1 Instrument Properties

An FX single pin barrier option is a single pin barrier option with the **cross currency** as the underlying. If we denote the **primary currency** per **cross currency** exchange rate on the **maturity date** by S_T , and the agreed **strike rate** by X, provided the appropriate barrier condition is met:

- 1) for a knock-out type option, the barrier is not touched on the barrier date, or
- 2) for a knock-in type option, the barrier is touched on the barrier date,

and the option expires in the money, in which a **call option** expires in the money if $S_T > X$ and a **put option** expires in the money if $S_T < X$, the holder of the **call option** (**put option**) buys (sells) the **cross currency amount**, denoted by N_c , at the predetermined **strike rate** X.

Provided either of the above barrier conditions holds, the payoff of an FX single pin barrier option is illustrated in Table 1.1.

Option Type	Expiry Condition	Payoff (primary currency)
Call	$S_T \le X$ $S_T > X$	$0 \ N_{ m c} \left(S_T - X ight)$
Put	$S_T \ge X$ $S_T < X$	$0 \ N_{ m c} \left(X - S_T ight)$

Table 1.1: Payoff at maturity for FX single pin barrier option if the underlying potion is active on the maturity date

1.2 Definitions

In this section, we define terms that are specific to FX single pin barrier options.

barrier is the primary currency per cross currency exchange rate level such that, if it is touched on the barrier date, the underlying option becomes active (inactive) for knock-in type (knock-out type) options.

barrier date is the date the barrier applies.

barrier direction is the direction that the barrier is considered to be touched.

call option gives the holder the right, but not the obligation, to buy the cross currency at the strike rate on the maturity date if the option is knocked-in (not knocked-out) for a knock-in type (knock-out type) option.

cross currency is the currency nominated as the underlying asset.

cross currency amount is the deal amount in cross currency that will be exchanged if the option is exercised.



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down is the barrier direction in cases where if the primary currency per cross currency exchange rate passes below the barrier on the barrier date, the barrier is considered to be touched.

knocked-in applies to knock-in type options and means the barrier was touched and the underlying option became active.

knocked-out applies to knock-out type options and means the barrier was touched and the underlying option became inactive.

knock-in type means the underlying option only becomes active if the barrier is touched on the barrier date.

knock-out type means the underlying option becomes inactive if the barrier is touched on the barrier date.

maturity date is the date the option expires.

primary currency is the currency that the deal is quoted in.

put option gives the holder the right, but not the obligation, to sell the **cross currency** at the **strike rate** on the **maturity date** if the option is **knocked-in** (not **knocked-out**) for a **knock-in type** (**knock-out type**) option.

strike rate is the agreed exchange rate between **primary currency** and **cross currency** if the option is exercised, quoted in **primary currency** per **cross currency**.

touched means for an option with an up (down) barrier, the primary currency per cross currency exchange rate was above (below) the barrier on the barrier date.

underlying option is the underlying FX vanilla option that specifies the payoff of the option should the option be either **knocked-in** or not **knocked-out**.

up is the barrier direction in cases where if the primary currency per cross currency exchange rate passes above the barrier on the barrier date, the barrier is considered to be touched.

1.3 Representations

In the Risk Engine, products are specified by *representations*. In this section, we provide the representations of FX single pin barrier options.

1.3.1 Default Representation

The Default representation consists of the mandatory trade fields in Table 1.2, with their restrictions in Table 1.3.

Field	Description	$Data\ Type$	Symbol
Currency	The primary currency	string	p
CrossCurrency	The cross currency	string	$^{\mathrm{c}}$
CurrencyAmount	The deal amount in <i>Currency</i>	double	$N_{ m p}$
CrossCurrencyAmount	The deal amount in CrossCurrency, i.e., the cross	double	$N_{ m c}$
	currency amount		
Barrier	The barrier level as Currency/CrossCurrency	double	H
BarrierDate	The date that the barrier applies, <i>i.e.</i> , the barrier date	date	BD
MaturityDate	The maturity date	date	MD
PutCall	Put option or call option on CrossCurrency	string	PC
UpDown	Direction of the barrier	string	UD
InOut	Knock-in option or knock-out option	string	IO
BoughtSold	Bought or sold the option	string	BS

Table 1.2: Mandatory trade fields for the Default representation of the FX Single Pin Barrier Option



Field	Restriction
CrossCurrency	$c \neq p$
CurrencyAmount	$N_{\rm p} > 0$
CrossCurrencyAmount	$N_{\rm c} > 0$
Barrier	H > 0
MaturityDate	MD > BD
PutCall	Put, Call, P, C
UpDown	Up, Down, U, D
InOut	In, Out, I, O
BoughtSold	Bought, Sold, B, S

Table 1.3: Trade field restrictions for the Default representation of the FX Single Pin Barrier Option

1.3.1.1 Required Curves

The following curves are required by an FX single pin barrier option:

- Currency FX spot curve: FX Spot Curve (FX.PRICE.Currency.BaseCurrency),
- CrossCurrency FX spot curve: FX Spot Curve (FX.PRICE.CrossCurrency.BaseCurrency),
- Currency discounting curve: FX Zero Curve (FX.ZERO.Currency.ReserveCurrency),
- CrossCurrency discounting curve: FX Zero Curve (FX.ZERO.CrossCurrency.ReserveCurrency), and
- Currency, CrossCurrency volatility grid: FX Volatility Grid (FX.GRID.CrossCurrency).

1.3.2 Strike Representation

The Strike representation consists of the mandatory trade fields in Table 1.4, with their restrictions in Table 1.5.

Field	Description	$Data\ Type$	Symbol
Currency	The primary currency	string	
CrossCurrency	The cross currency	string	$^{\mathrm{c}}$
${\bf CrossCurrencyAmount}$	The deal amount in CrossCurrency, i.e., the cross	double	$N_{ m c}$
	currency amount		
Strike	The strike rate as Currency/CrossCurrency	double	X
Barrier	The barrier level as Currency/CrossCurrency	double	H
BarrierDate	The date that the barrier applies, <i>i.e.</i> , the barrier date	date	BD
MaturityDate	The maturity date	date	MD
PutCall	Put option or call option on CrossCurrency	string	PC
UpDown	Direction of the barrier	string	UD
InOut	Knock-in option or knock-out option	string	IO
BoughtSold	Bought or sold the option	string	BS

Table 1.4: Mandatory trade fields for the Strike representation of the FX Single Pin Barrier Option

1.3.2.1 Required Curves

The following curves are required by an FX single pin barrier option:

- Currency FX spot curve: FX Spot Curve (FX.PRICE.Currency.BaseCurrency),
- CrossCurrency FX spot curve: FX Spot Curve (FX.PRICE.CrossCurrency.BaseCurrency),
- Currency discounting curve: FX Zero Curve (FX.ZERO.Currency.ReserveCurrency),
- Currency, CrossCurrency volatility grid: FX Volatility Grid (FX.GRID.CrossCurrency.Currency).



1.4. Formula 7

Field	Restriction
CrossCurrency	$c \neq p$
CrossCurrencyAmount	$N_{\rm c} > 0$
Strike	X > 0
Barrier	H > 0
MaturityDate	MD > BD
PutCall	Put, Call, P, C
UpDown	Up, Down, U, D
InOut	In, Out, I, O
BoughtSold	Bought, Sold, B, S

Table 1.5: Trade field restrictions for the Strike representation of the FX Single Pin Barrier Option

1.4 Formula

If the Valuation Date is less than or equal to the **maturity date**, the value of an FX single pin barrier option in Base Currency is given by the FX single pin barrier option pricing function¹,

FXSinglePinBarrier
$$(E_p, E_c, X, N_c, H, r_{p,1}, r_{c,1}, \sigma_1, t_1, r_{p,2}, r_{c,2}, \sigma_2, T_2, indicator),$$
 (1.1)

where

- $E_{\rm p}$ is the spot exchange rate in units of Base Currency per **primary currency**, from the Currency FX spot curve,
- E_c is the spot exchange rate in units of Base Currency per **cross currency**, from the CrossCurrency FX spot curve.
- X is the strike rate in units of primary currency per cross currency,
- N_c is the cross currency amount,
- H is the barrier level in units of primary currency per cross currency,
- $r_{p,1}$ is the cross currency basis adjusted continuous zero rate of **primary currency** from Valuation Date to **barrier date** in Actual/365 (Fixed) day count convention, from the Currency discounting curve,
- $r_{c,1}$ is the cross currency basis adjusted continuous zero rate of **cross currency** from Valuation Date to **barrier date** in Actual/365 (Fixed) day count convention, from the CrossCurrency discounting curve,
- σ_1 is the volatility of the exchange rate between **primary currency** and **cross currency** from Valuation Date to **barrier date** in Actual/365 (Fixed) day count convention, from the Currency, CrossCurrency volatility grid,
- t_1 is the time in years from Valuation Date to barrier date in Actual/365 (Fixed) day count convention,
- $r_{\rm p,2}$ is the cross currency basis adjusted continuous zero rate of **primary currency** from Valuation Date to **maturity date** in Actual/365 (Fixed) day count convention, from the Currency discounting curve,
- r_{c,2} is the cross currency basis adjusted continuous zero rate of cross currency from Valuation Date to maturity
 date in Actual/365 (Fixed) day count convention, from the CrossCurrency discounting curve,
- σ₂ is the volatility of the exchange rate between primary currency and cross currency from Valuation Date
 to maturity date in Actual/365 (Fixed) day count convention, from the Currency, CrossCurrency volatility
 grid,
- T₂ is the time in years from Valuation Date to maturity date in Actual/365 (Fixed) day count convention, and
- indicator contains the put/call, up/down, in/out and bought/sold information.

If the Valuation Date is greater than the **maturity date**, then the FX single pin barrier option has expired and thus has a value of zero.



¹See FX Single Pin Barrier Option Pricing for details (p.10 of this document).

1.4.1 Representation Reduction

Equation (1.1) is only defined for the Strike representation. If the trade is specified by other representations, we need to reduce it to the Strike representation.

1.4.1.1 Default Representation

For the Default representation, the \mathbf{strike} \mathbf{rate} , X, is the ratio of CurrencyAmount and CrossCurrencyAmount, given by

 $X = \frac{N_{\rm p}}{N_{\rm c}}.\tag{1.2}$

1.5 Examples

This section provides some deal examples of FX single pin barrier option.

Example 1.1. An FX single pin barrier option in Default representation:

Currency: AUDCrossCurrency: GBP

CurrencyAmount: 100,000,000CrossCurrencyAmount: 60,000,000

• Barrier: 1.6725

BarrierDate: 2013-10-15MaturityDate: 2013-11-15

PutCall: PutUpDown: UpInOut: Out

• BoughtSold: Bought

Using equation (1.2), the **strike rate** of the option is

$$X = \frac{N_{\rm p}}{N_{\rm c}} = \frac{100,000,000}{60,000,000} = 1.6667.$$

a) If on 2013-11-15, the option expires in the money with the AUD/GBP exchange rate being 1.6515, with the AUD/GBP exchange rate was below the **barrier** (1.6725) on 2013-10-15, the payoff of the option is

$$N_{\rm c}(X - S_T) = 60,000,000 \times (1.6667 - 1.6515) = \$910,000 \text{ AUD}.$$

- b) If on 2013-11-15, the option expires out of the money with the AUD/GBP exchange rate being 1.6715, with the AUD/GBP exchange rate was below the **barrier** (1.6725) on 2013-10-15, the payoff of the option is 0 as the **strike** rate (1.6667) is less than the AUD/GBP exchange rate (1.6715) on the **maturity date**.
- c) If the AUD/GBP exchange rate passed above the **barrier** (1.6725) on 2013-10-15, the option was **knocked-out** because the **barrier** was **touched** on the **barrier date**, thus the payoff of the option is 0.

Example 1.2. An FX single pin barrier option in Strike representation:

• Currency: JPY

• CrossCurrency: USD

• CrossCurrencyAmount: 100,000,000

Strike: 100.2Barrier: 97.5

BarrierDate: 2013-10-15MaturityDate: 2013-11-15

PutCall: CallUpDown: Down

• InOut: In

• BoughtSold: Bought

a) If on 2013-11-15, the option expires in the money with the JPY/USD exchange rate being 102.5, with the JPY/USD exchange rate was below the **barrier** (97.5) on 2013-10-15, the payoff of the option is

$$N_c(S_T - X) = 100,000,000 \times (102.5 - 100.2) = $230,000,000 \text{ JPY}.$$



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b) If on 2013-11-15, the option expires out of the money with the JPY/USD exchange rate being 98.4, with the JPY/USD exchange rate was below the **barrier** (97.5) on 2013-10-15, the payoff of the option is 0 as the **strike** rate (100.2) is greater than the JPY/USD exchange rate (98.4) on the **maturity date**.

c) If the JPY/USD exchange rate was above the **barrier** (97.5) on 2013-10-15, the option was not **knocked-in** because the **barrier** was not **touched** on the **barrier date**, thus the payoff of the option is 0.



Chapter 2

FX Single Pin Barrier Option Pricing

2.1 Inputs to Function

Description	Symbol	min	max	Reasonable range
Spot rate of primary currency	$E_{\rm p}$	0+	$+\infty$	
Spot rate of cross currency	$E_{ m c}$	0_{+}	$+\infty$	
Strike rate as primary currency/cross currency	X	0_{+}	$+\infty$	
Cross currency amount	$N_{ m c}$	0_{+}	$+\infty$	
Barrier as primary currency/cross-currency	H	0_{+}	$+\infty$	
Continuous zero rate of primary currency till t_1	$r_{ m p,1}$	0+	$+\infty$	
Continuous zero rate of cross currency till t_1	$r_{ m c,1}$	0+	$+\infty$	
Volatility of exchange rate between primary and cross currencies	σ_1	0+	$+\infty$	
$\operatorname{till}t_1$				
Time from value date to barrier date in years	t_1	0_{+}	$< T_2$	
Continuous zero rate of primary currency till T_2	$r_{\mathrm{p},2}$	0_{+}	$+\infty$	
Continuous zero rate of cross currency till T_2	$r_{ m c,2}$	0_{+}	$+\infty$	
Volatility of exchange rate between primary and cross currencies	σ_2	0_{+}	$+\infty$	
$\operatorname{till} T_2$				
Time from value date to maturity in years	T_2	$> t_1$	$+\infty$	
Put or Call		_	_	"P", "C"
Up or Down	: 1: 4	_	_	"U", "D"
In or Out	indicator	_	_	"I", "O"
Bought or Sold		_	_	"B", "S"

Table 2.1: Inputs for FX Single Pin Barrier Option pricing function

2.2 Formula

The spot exchange rate of primary currency per cross currency is given by

$$S = \frac{E_{\rm c}}{E_{\rm p}}.$$

We can value an FX single pin barrier option by calling the $single\ pin\ barrier\ pricing\ function^1$ with appropriate inputs. The value of an FX single pin barrier option in Base Currency is

$$N_{\rm c} \times E_{\rm p} \times \mathbb{I}_{\rm BS} \times {\rm SinglePinBarrier}\left(S, X, H, r_{\rm p,1}, r_{\rm c,1}, \sigma_1, t_1, r_{\rm p,2}, r_{\rm c,2}, \sigma_2, T_2, {\rm indicator}\right),$$

¹See pricing specification Single Pin Barrier Option for details.



2.2. Formula 11

 $\quad \text{where} \quad$

$$\mathbb{I}_{BS} = \begin{cases} 1, & \text{if indicator is 'B',} \\ -1, & \text{if indicator is 'S'.} \end{cases}$$



Glossary

Base Currency The currency that the risk engine is configured to return values in.

Reserve Currency The currency that all cross currency basis is benchmarked against.

 ${\bf Risk\ Engine}\,$ The Vector Risk market risk and credit risk system.

Valuation Date The date that we value the trades as.

